## GENERAL EQUILIBRIUM - EDGEWORTH BOX AND WELFARE ECONOMICS

## Problem \#1

Is it true that if two consumers have identical preferences, then the contract curve linking all efficient allocations is a straight line?

## Problem \#1

Paul's utility function is given by the formula $U_{\mathrm{P}}\left(x_{\mathrm{P} 1}, x_{\mathrm{P} 2}\right)=x_{\mathrm{P} 1}{ }^{1 / 3}{ }_{X_{\mathrm{P} 2}}{ }^{2 / 3}$ and John's utility function is $U_{\mathrm{J}}\left(x_{\mathrm{J} 1}\right.$, $\left.x_{\mathrm{J} 2}\right)=x_{\mathrm{J} 1}{ }^{1 / 2} x_{\mathrm{J} 2}{ }^{1 / 2}$. Paul disposes of an initial endowment $\omega_{\mathrm{P} 1}=1$ and $\omega_{\mathrm{P} 2}=0$, while for John it is $\omega_{\mathrm{J} 1}=0$ and $\omega_{\mathrm{J} 2}=1$. Their only income comes from selling some of the initial endowments. Assuming that prices $p_{1}$ and $p_{2}$ of goods $x_{1}$ and $x_{2}$ are determined by an impartial arbiter-auctioneer, at what ratio of these prices will the equilibrium for the exchange between Paul and John take place?

## Problem \#2

Within the Edgeworth box, is the Pareto set always a certain curve, where a given allocation of one good corresponds to precisely one allocation of the other good? Provide a reasoning for your answer.

## Problem \#3

Is it possible that a consumer is worse-off in a Pareto-optimal situation than in a setting which is not Pareto-optimal? Provide a reasoning for your answer.

## Problem \#4

A pair of earrings and a necklace are complementary goods for Margaret. For John, who does not really care about harmony, a single earring and a necklace are perfect substitutes and he values a single earring and a necklace identically. There are 4 necklaces and 2 pairs of earrings. From the Edgeworth box it can be seen that allocation (1,2) (i.e. 1 necklace and 2 earrings for Margaret, 3 necklaces and 2 earrings for John) is Pareto-optimal. Find the price ratio and initial allocation of the two goods between John and Margaret, for which the discussed allocation would be the market equilibrium.

## Problem \#5

Why equilibrium in a market where certain products are supplied by monopolists who do not apply price differentiation is not Pareto-optimal (when demand decreases together with increase in the price)?

## Problem \#6

Is it possible to prove the Second Theorem of Welfare Economics for a monopolist applying price differentiation?

## Problem \#7

The value of excess demands in five markets out of seven is equal to zero. What can we say about the remaining two markets?

